

# To Zoom or Not to Zoom?

## *A Numerical Study of Excess Airspeed After Engine Failure*

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### Abstract

After an engine failure, pilots are commonly taught to establish best-glide speed. A less clearly answered question is what to do when the airplane is initially traveling substantially faster than best glide. Should the pilot remain level and allow drag to remove the excess speed, or should some of that kinetic energy be converted into altitude through a zoom maneuver? The usual arguments are intuitive but incomplete because the result depends not simply on how quickly the airplane slows, but on the drag accumulated along the complete trajectory from the initial engine failure to the final steady glide.

A numerical point-mass simulation was developed in MATLAB to compare these trajectories on equal terms. Both the zoom and level-deceleration cases were required to reach the same final best-glide speed and flight-path angle, including the finite maneuver required to establish that glide. For a representative Cessna-172-like case beginning at 110 knots and transitioning to a 65-knot best glide, the mathematically optimized zoom retained approximately 260 ft of additional eventual still-air glide range. This advantage was real but modest. The result was also highly dependent on how the maneuver was completed: an excessively gentle transition reduced the benefit, while waiting until the airplane had already reached best-glide speed before beginning the pushover produced a substantial underspeed excursion before the glide could be established.

A broader analysis showed that the usefulness of a zoom is governed more by initial speed relative to the airplane's own best-glide speed than by absolute airspeed alone. The benefit approaches zero as initial speed approaches best-glide speed and increases smoothly as the ratio of initial speed to best-glide speed increases. Higher aerodynamic efficiency also increases the value of preserving energy as altitude. Thus, the trainer case lies in a weak-benefit regime, while substantially higher excess-speed ratios can produce much larger gains. Larger or faster airplanes should not automatically be considered better zoom candidates, however, because they generally also have higher best-glide speeds. Numerical convergence, independent dimensional and normalized formulations, multiple optimizer starts, and sensitivity studies supported these trends; the high-energy results became increasingly dependent on allowable maneuver limits rather than maximum lift capability.

The study does not prescribe an emergency maneuver. In the trainer regime, the aerodynamic advantage can be small enough that execution error, wind, pilot workload, and the opportunity cost of attention may equal or exceed the theoretical gain. A trajectory that preserves more aircraft energy may still leave the pilot less able to select a landing site, troubleshoot the failure, configure the airplane, or communicate. The broader conclusion is therefore not simply "zoom" or "do not zoom," but that excess airspeed after a loss of thrust is a constrained trajectory problem whose practical answer depends on the aircraft's energy state, aerodynamic efficiency, maneuver constraints, and pilot execution.

### 1. The Question

Imagine a light airplane cruising in level flight at 110 knots when the engine suddenly stops producing thrust. Best-glide speed is 65 knots. The airplane now contains more kinetic energy than it needs for the steady best-glide condition. What should happen to that energy?

One option is straightforward: maintain approximately level flight and allow drag to decelerate the airplane from 110 to 65 knots. Another is to pitch up, converting some of the excess kinetic energy into altitude, and then transition into the best glide.

This question can generate surprisingly strong opinions. A common argument for zooming is that drag, particularly parasite drag, is high at high speed. Therefore, the airplane should spend as little time as possible at high speed, converting some of that excess airspeed into altitude through a zoom. There is truth in that observation, but it does not by itself determine the optimum trajectory.

A representative pilot-oriented statement of this energy argument appears in John S. Denker's *See How It Flies*. In his engine-out discussion, Denker notes that remaining well above best-glide speed throws energy away through unnecessary parasite drag and advises the pilot to “gently zoom upward, converting airspeed to altitude” [1]. The energy logic is sound, but the word “gentle” leaves the trajectory itself undefined. The present study therefore asks a narrower question: how should the complete transition be flown, and how much does the answer matter in the relatively low-excess-energy regime occupied by common trainers?

The airplane's specific mechanical energy can be written as

$$E = h + V^2 / (2g) \quad (1)$$

where  $h$  is altitude and  $V^2/(2g)$  is the kinetic-energy equivalent expressed as a height. After thrust is lost, aerodynamic drag continually removes mechanical energy:

$$\dot{E} = -DV / W \quad (2)$$

The question is therefore not merely how quickly the airspeed decreases. It is how much energy is lost to drag over the entire trajectory while the airplane transitions from its initial condition to steady best glide. A level deceleration turns essentially all of the excess kinetic energy into drag loss, whereas a zoom attempts to divide that energy between altitude gain and drag loss. Whether that is worthwhile depends on what it costs to perform the maneuver.

## 2. Relationship to Prior Work

The underlying optimization problem is not new. Shapira and Ben-Asher directly studied an engine-cutoff case beginning at high velocity and low altitude, formulating the initial transient as a fast dynamic phase in which excess airspeed is converted into altitude and range before the aircraft settles into a classical quasi-steady glide [2]. Their work, demonstrated with an F-16 model, is a closely related technical precedent for the specific excess-speed question considered here.

Related work has treated broader engine-out and unpowered-flight optimization problems. Atkins, Portillo, and Strube developed emergency flight-planning methods for total loss of thrust [3]; Wolek, Cliff, and Woolsey formulated energy-optimal glider paths using speed and load factor as controls [4]; and Segal, Bar-Gill, and Shimkin derived maximum-range engine-out glide solutions in severe wind and demonstrated them using a Cessna 172 model [5]. The present study does not claim novelty in the idea of converting excess speed into altitude. Its narrower aim is to examine the pilot-training question as a complete state-to-state maneuver, quantify the sensitivity to pull-up and pushover execution, identify the weak-benefit trainer regime, and map how that benefit changes with  $V_0/V_{BG}$  and maximum glide ratio.

## 3. A Simple Numerical Airplane

The initial study used a deliberately simple Cessna-172-like point-mass airplane rather than attempting to reproduce a particular serial number or flight-test dataset. The principal state variables were

$$x, h, V, \gamma$$

representing horizontal position, altitude, true airspeed, and flight-path angle. The equations of motion were

$$\dot{x} = V \cos \gamma \quad (3a)$$

$$\dot{h} = V \sin \gamma \quad (3b)$$

$$\dot{V} = -D/m - g \sin \gamma \quad (3c)$$

$$\dot{\gamma} = (g/V)(n - \cos \gamma) \quad (3d)$$

where  $n$  is load factor. Aerodynamic drag was represented by a conventional parabolic drag polar,

$$C_D = C_{D0} + k C_L^2 \quad (4)$$

Lift coefficient was calculated from the load factor required by the maneuver:

$$C_L = nW / (qS) \quad (5)$$

The model also explicitly integrated the energy dissipated by drag. This provided a useful numerical check:

$$h + V^2/(2g) + H_D = \text{constant} \quad (6)$$

where  $H_D$  is cumulative drag loss expressed as an equivalent height. If that relationship failed to remain constant, something was wrong with either the equations or their numerical implementation. For the initial experiment, the airplane began at 110 knots and the target best-glide speed was 65 knots, with an assumed maximum lift-to-drag ratio of approximately 9:1. The effective parabolic drag polar was constructed by requiring the specified 65-kt condition to coincide with  $(L/D)_{\max} = 9.0$ , which uniquely determines  $C_{D0}$  and  $k$  for the assumed weight, wing area, and atmospheric density.

Table 1. Nominal C172-like model and production maneuver constraints.

| Quantity                         | Nominal value                                                                                                 | Purpose / note                                                                                                        |
|----------------------------------|---------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------|
| Representative weight            | 2,300 lb                                                                                                      | Chosen operating weight; not a claim of exact aircraft test condition.                                                |
| Wing area, $S$                   | 174 ft <sup>2</sup>                                                                                           | C172-like reference geometry.                                                                                         |
| Air density, $\rho$              | 0.00237 slug/ft <sup>3</sup>                                                                                  | Sea-level standard atmosphere.                                                                                        |
| Best-glide speed, $V_{BG}$       | 65 kt                                                                                                         | Reference terminal speed for the nominal case.                                                                        |
| Maximum glide ratio              | 9.0                                                                                                           | Effective engine-out L/D used to construct the polar.                                                                 |
| Maximum lift coefficient         | 1.50                                                                                                          | Feasibility / stall constraint.                                                                                       |
| Effective drag polar             | $C_D = 0.05134 + 0.06012 C_L^2$                                                                               | Derived so 65 kt occurs at maximum L/D = 9.0.                                                                         |
| Lift-capability ratio, $\lambda$ | 1.62317                                                                                                       | $\lambda = CL_{\max} / CL^*$ .                                                                                        |
| Nominal maneuver bounds          | $n_{\text{pull}} \leq 3.8$ ; $\gamma_{\text{zoom}} \leq 25^\circ$ ;<br>$0.30 \leq n_{\text{push}} \leq 0.975$ | Production optimization limits; the coarse pushover grid sampled 0.30–0.95, with local refinement permitted to 0.975. |

For every comparison, both the zoom trajectory and the no-zoom baseline were required to physically reach the same terminal state,  $V = V_{BG}$  and  $\gamma = \gamma_{BG}$ . The baseline therefore receives no free or instantaneous change from level flight into the glide. Once that common state is reached, eventual air-relative range can be scored by adding the downrange distance already traveled to the steady-glide range represented by the remaining altitude:

$$J = x_f + h_f \cot(-\gamma_{BG}) \quad (7)$$

Here,  $h_f$  is measured relative to the engine-failure altitude datum. The quantity optimized throughout the study is the difference between the best zoom trajectory and the best no-zoom trajectory:

$$\Delta J = J_{\text{zoom,opt}} - J_{\text{no-zoom,opt}} \quad (8)$$

This definition keeps the path in the problem:  $J$  is evaluated only after the complete maneuver has been integrated. It is not calculated by assuming an ideal conversion of kinetic energy into altitude.

The production study integrated the complete nondimensional point-mass equations using MATLAB's ode45, with terminal event detection defining transitions among the pull-up, constant-flight-path-angle zoom, and finite pushover phases and enforcing the common endpoint at normalized best-glide speed and flight-path angle. The earlier trainer study used direct parameter sweeps, while the generalized

regime map evaluated each candidate through full numerical integration using a coarse maneuver-parameter grid followed by bounded local grid refinement about the best solution. No analytical energy shortcut or neighboring-point warm start was used; the contours therefore represent independently optimized outer-grid points. Feasibility was determined from maneuver bounds, lift capability, available entry speed, phase-completion requirements, and terminal tolerances, with invalid candidates rejected. Selected solutions were subsequently recomputed at higher fidelity using tighter integration tolerances and a bounded derivative-free coordinate search from multiple initial conditions, with convergence and multistart checks used to assess sensitivity to numerical resolution and local optima.

#### 4. The First Comparison

The first version compared two basic strategies. The baseline simply remained level while the airplane slowed from 110 knots to 65 knots. The zoom maneuver consisted of:

1. pulling at a selected load factor,
2. reaching a selected positive flight-path angle,
3. maintaining that climb angle while the airplane decelerated,
4. and ending the calculation when 65 knots was reached.

The computer swept through combinations of pull-up load factor and zoom angle to determine which retained the greatest eventual range. An early result showed that a moderate zoom could outperform level deceleration. With the assumed airplane, the optimum appeared near a 2-g pull and a climb angle of roughly 14 to 15 degrees.

That was interesting, but the comparison contained an important flaw. The level case reached 65 knots while traveling level, while the zoom case reached 65 knots while still climbing. Those were not the same terminal states. Giving the zoom airplane credit for its additional altitude without charging it for the maneuver required to rotate into the descending best-glide flight path unfairly favored the zoom. That led to the first major refinement.

#### 5. The Pushover Matters

The next model required every trajectory to finish at the same state:

$$V = 65 \text{ knots}, \quad \gamma = \gamma_{BG}$$

where  $\gamma_{BG}$  was the steady best-glide descent angle. The zoom maneuver therefore became:

*pull -> zoom -> pushover -> steady best glide*

This changed the problem substantially. A shallow zoom requires only a small change in flight-path angle before reaching the glide, whereas a steep zoom requires a much larger rotation from a positive climb angle to a negative glide angle. That transition costs time, distance, and energy.

The pushover was described by a load factor below 1 g. A lower load factor produces a more aggressive downward rotation of the flight path, while a load factor close to 1 g produces a gentle transition. The numerical results showed that the pushover was not a minor detail; it was one of the dominant features of the problem. For the 110-knot case, the best overall results occurred with a pushover of roughly 0.7 to 0.8 g, while the optimum remained near a 2-g pull and approximately 14 to 15 degrees of zoom angle.

Under the assumptions of the model, the best trajectory retained approximately 260 feet more eventual still-air glide range than simply decelerating level. That number should be kept in perspective: at a 9:1 glide ratio, 260 feet of eventual range is equivalent to only about 29 feet of additional best-glide altitude. The theoretical benefit was therefore real, but modest. Figure 1 shows the complete nominal trajectories and their common best-glide continuation using equal horizontal and vertical physical scaling.

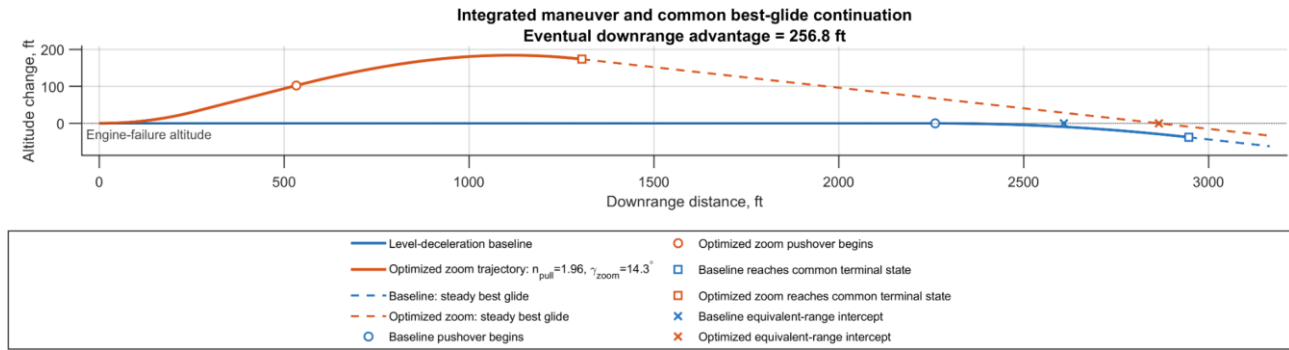


Figure 1. Nominal trainer-case trajectories with a common terminal state. The level-deceleration baseline and optimized zoom begin from the same 110-kt power-off condition and are integrated until both reach the same 65-kt steady best-glide state. The optimized trajectory uses  $n_{pull} = 1.96$  and  $\gamma_{zoom} = 14.3^\circ$ . Dashed lines show the common steady best-glide continuation; the optimized zoom produces an eventual downrange advantage of 256.8 ft in the model. Horizontal and vertical axes use equal physical scaling.

More interesting than the exact number was what happened when the pushover became gentler. At a pushover near 0.95 g, the optimum zoom angle collapsed to only a few degrees because the airplane had to begin transitioning toward the glide so early that little useful zoom remained. The result therefore indicates that if the pilot intends to make a gentle transition into the glide, the airplane should not be zoomed very much in the first place. This result also qualifies the otherwise sensible pilot guidance to “gently zoom upward” [1]. The model supports the underlying energy conversion, but shows that gentle is not by itself a sufficient trajectory prescription: an overly mild complete transition can preserve little of the available advantage, particularly in the trainer-like regime where the ideal benefit is already small.

This behavior follows directly from Eq. (3d). Near level flight, a 0.95-g maneuver generates very little downward rotation, while a 0.75-g maneuver rotates the flight path much more rapidly. The practical implication is not that the pilot should make the most abrupt possible pushover; the optimization showed a broad optimum rather than favoring the lowest possible load factor. Instead, a useful zoom requires remaining in the energy-conversion portion of the maneuver relatively late and then making a sufficiently decisive transition into the glide.

## 6. Pushover Timing and Airspeed Undershoot

This led to the next question: what happens if the pilot waits too long?

Suppose the ideal trajectory calls for beginning the pushover at approximately 83 knots. A pilot who is focused primarily on the published 65-knot best-glide speed might wait until the airspeed indicator actually reaches 65 knots before lowering the nose. The simulation showed why this can be a serious mistake. Airspeed does not stop decreasing simply because it passes through best-glide speed; if the airplane is still climbing while the pilot begins the pushover, kinetic energy continues to be converted into altitude while the flight path rotates downward.

In the nominal model, beginning the pushover near 83 knots allowed the airplane to arrive at the final glide at approximately 65 knots. Waiting until 65 knots to begin the pushover resulted in the airplane decelerating to roughly 51 knots before the maneuver bottomed out and airspeed began recovering. This is an important distinction: best-glide speed may be the desired speed at the end of the transition, not necessarily the correct speed at which to begin the transition.

The simulation also imposed a maximum lift coefficient so that the airplane could not simply generate whatever load factor the commanded maneuver demanded. As the pilot delayed the pushover farther and farther, the resulting underspeed eventually drove the maneuver toward the airplane's aerodynamic limits. Interestingly, the theoretical range advantage did not immediately disappear when

the pilot made a timing error; some imperfectly timed zooms still retained slightly more calculated range than level deceleration. That does not make them desirable. The airplane could retain a theoretical energy advantage while simultaneously entering a very slow and increasingly demanding recovery, highlighting an important difference between an energetically favorable trajectory and a sensible pilot technique.

## 7. Wind Changes the Ground-Range Question

Uniform wind does not directly alter the airplane's aerodynamic energy state relative to the surrounding airmass; the airplane still experiences the same lift, drag, and airspeed. Ground distance, however, depends on elapsed time. The ground-relative horizontal velocity is

$$\dot{x}_g = V \cos \gamma + W \quad (9)$$

where  $W$  is the wind component, positive for a tailwind. The optimized zoom trajectory generally spends more time airborne during the transition than the level-deceleration trajectory, so the two paths experience different amounts of wind displacement before reaching the same final glide state.

For the nominal 110-knot case, under the fixed 65-knot terminal best-glide condition used in this study, the simulation produced a ground-range break-even point at approximately a 26-knot headwind. With no wind, the previously established still-air advantage remained. As the headwind increased, that advantage decreased; around a 26-knot headwind, the two strategies became approximately equal in ground range, and with a stronger headwind the level-deceleration trajectory could outperform the zoom over the ground. A tailwind had the opposite effect. The study did not re-optimize the subsequent steady-glide airspeed for wind, so this break-even value should be interpreted as a comparison of the transition trajectories under a common fixed terminal-glide condition rather than as a general maximum-ground-range result in wind.

This does not mean the wind changed the aerodynamic efficiency of the zoom. It changed the value of time spent airborne in a moving airmass. Again, the result argues against universal slogans: determining which trajectory produces greater ground range requires specifying both the reference frame and the terminal glide condition.

## 8. Initial Airspeed Changes Everything

Perhaps the clearest result appeared when the same conceptual experiment was repeated from a much higher initial speed. The available excess kinetic energy is

$$\Delta E_k = \frac{1}{2} m (V_0^2 - V_{BG}^2) \quad (10)$$

Because kinetic energy depends on the square of velocity, increasing the initial speed creates a disproportionately larger energy reservoir. For the simplified model, the excess kinetic-energy equivalent between 110 and 65 knots was on the order of a few hundred feet, while beginning at 200 knots instead produced well over a thousand feet. Not surprisingly, the value of converting some of that energy into altitude increased dramatically.

In fact, when the 172-like mathematical model was artificially started at 200 knots, the optimization drove toward the edges of the selected search space: higher pull load factors and steeper zoom angles continued to improve the calculated result. That particular calculation should not be mistaken for a recommendation involving a real Cessna 172; a 172 is not the airplane with which to explore a 200-knot, multi-g engine-failure maneuver. The purpose of the experiment was to examine the scaling of the physics. It showed that the significance of the zoom can change substantially when the initial airspeed is much farther above the airplane's best-glide speed.

This may help explain why seemingly contradictory intuitions about zoom climbs can both sound reasonable. For a typical trainer, the theoretical advantage may be limited and may be strongly affected

by pilot execution. For an airplane traveling far above its eventual glide speed, simply dissipating all of its excess kinetic energy as drag can potentially throw away a much larger resource.

This suggested that the more useful organizing variable is not aircraft type or absolute speed by itself, but the ratio of the initial speed to the airplane's own best-glide speed:

$$u_0 = V_0 / V_{BG} \quad (11)$$

That observation motivated a second study in which the named airplane was temporarily removed from the problem and the trajectory optimization was repeated across a generic family of parabolic-polar airplanes.

### 9. A General Nondimensional Regime Map

The generalized study swept initial-speed ratio  $u_0$  from just above 1 to approximately 4 and maximum glide ratio from 5 to 20. At each point, the complete trajectory was re-optimized over pull load factor, zoom angle, and pushover load factor while retaining the common terminal state. The resulting surface is smooth: the zoom advantage approaches zero as  $u_0$  approaches one, then grows continuously as excess-speed ratio and aerodynamic efficiency increase. There is no sharp aerodynamic line at which zooming suddenly becomes beneficial; instead, there is a progression from negligible benefit to a strong energy-conversion regime.

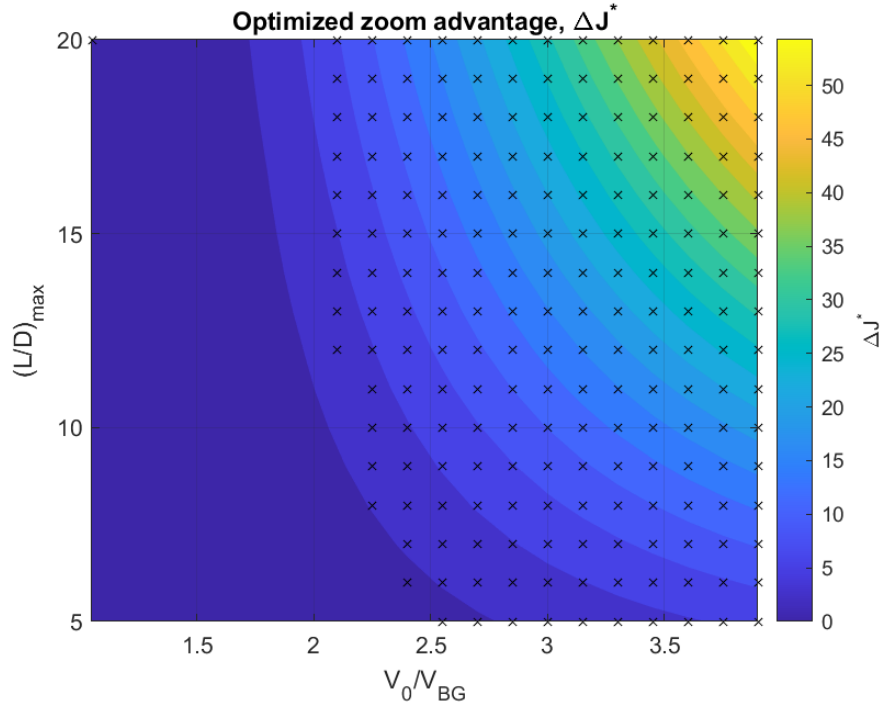


Figure 2. Optimized nondimensional zoom advantage across initial-speed ratio and maximum glide ratio. Crosses indicate computed grid points. The benefit is negligible near  $V_0/V_{BG} = 1$  and increases smoothly with both excess-speed ratio and aerodynamic efficiency.

Figure 2 changes the interpretation of the original trainer result. The 110-to-65-kt case has  $u_0 \approx 1.7$  and  $L/D \approx 9$ , placing it in a region where the mathematical optimum includes a zoom but the absolute benefit is modest. At much larger speed ratios, particularly for efficient airplanes, the available kinetic-energy reservoir grows rapidly and the penalty for dissipating it directly through drag becomes much larger.

To compare the magnitude of the advantage with the ideal range value of the available excess kinetic energy, the study also used the dimensionless preserved-energy metric

$$\eta_{\text{pres}} = \Delta J^* / [(L/D)_{\text{max}} (u_0^2 - 1)/2] \quad (12)$$

where  $\Delta J^*$  is the normalized range advantage. This quantity does not represent total glide efficiency; it asks how much of the ideal range value of the initial excess kinetic energy is preserved by the optimized zoom relative to the optimized no-zoom baseline. Across the production map it remained between zero and 0.40.

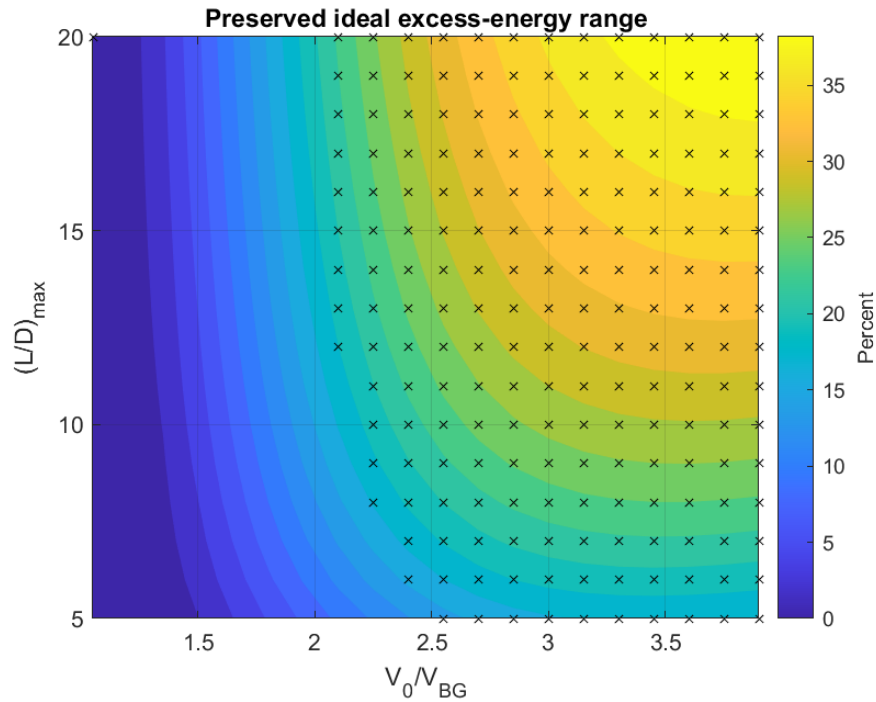


Figure 3. Fraction of the ideal excess-energy range preserved by the optimized zoom, expressed as a percentage. The metric remains small in trainer-like conditions and grows into the tens of percent at high speed ratios and high  $L/D$ .

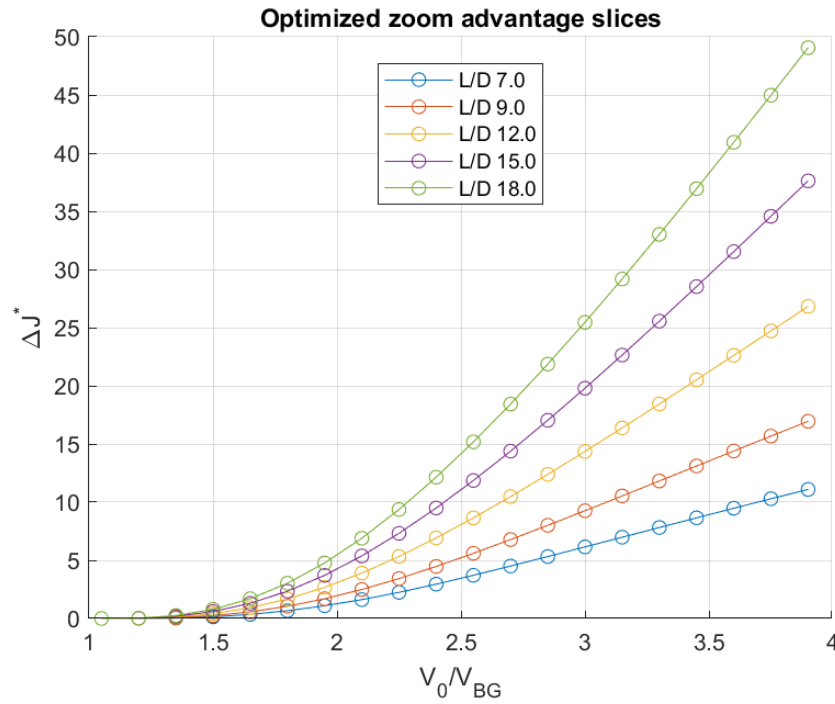


Figure 4. Optimized zoom-advantage slices for selected glide ratios. The smooth curves make the regime behavior particularly clear: advantage approaches zero near best-glide speed and increases progressively with  $V_0/V_{BG}$ , with larger gains for more aerodynamically efficient airplanes.

The optimized control histories also change systematically with regime. At low excess-speed ratios, the best maneuver collapses toward a shallow, low-load-factor transition. As  $u_0$  increases, the optimizer requests progressively larger pull load factors and zoom angles. In the high-speed portion of the production map, both pull load factor and zoom angle reach the imposed 3.8-g and 25-degree limits. Those regions therefore represent the best trajectories permitted by the selected maneuver box, not an unconstrained optimum. Pushover load factor remains an interior variable over the tested production cases.

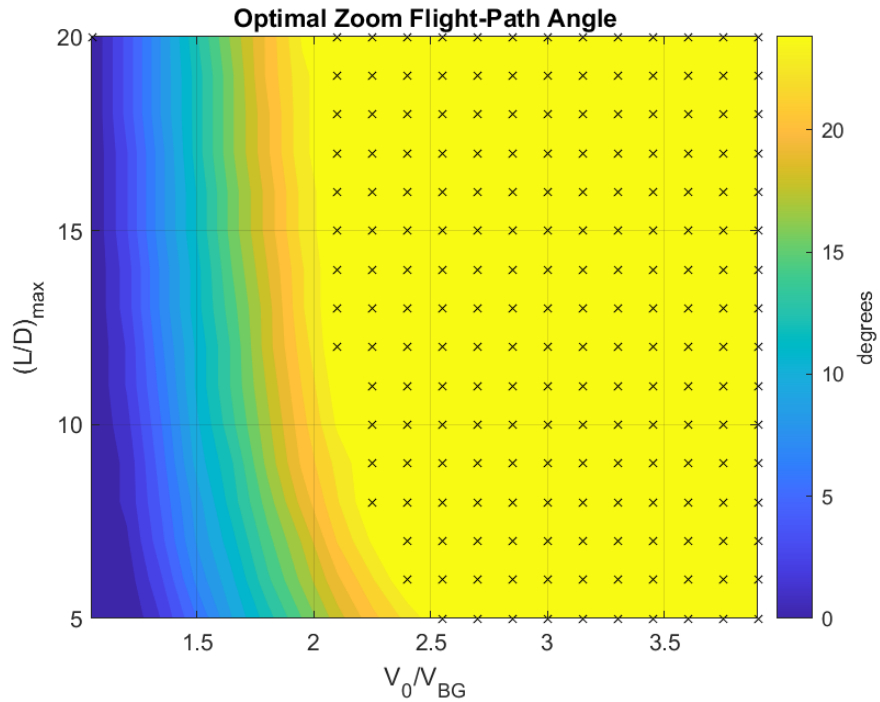


Figure 5(a). Optimal zoom flight-path angle across the nondimensional regime map.

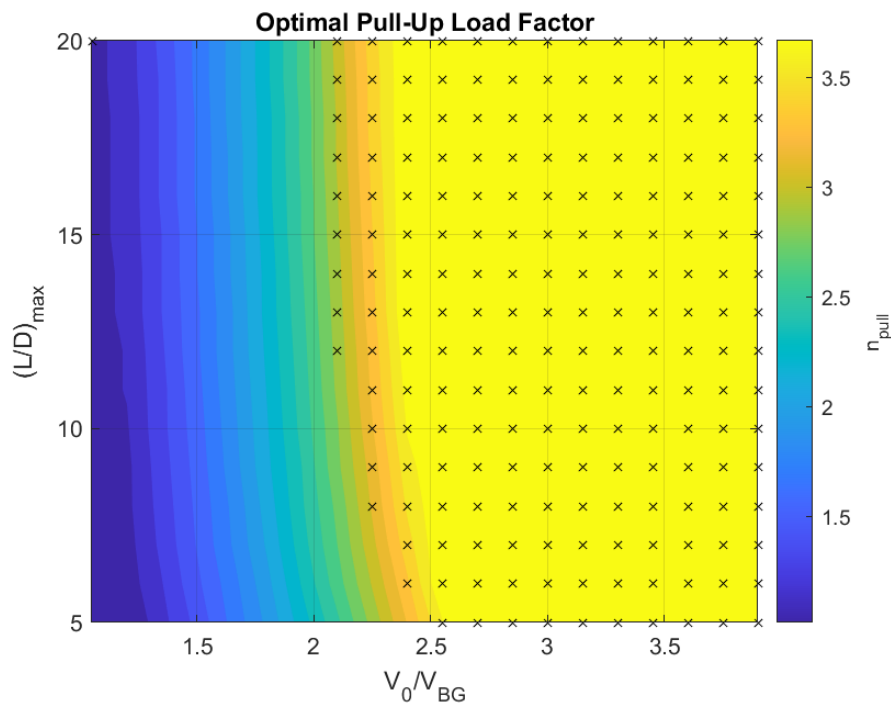


Figure 5(b). Optimal pull-up load factor across the nondimensional regime map.

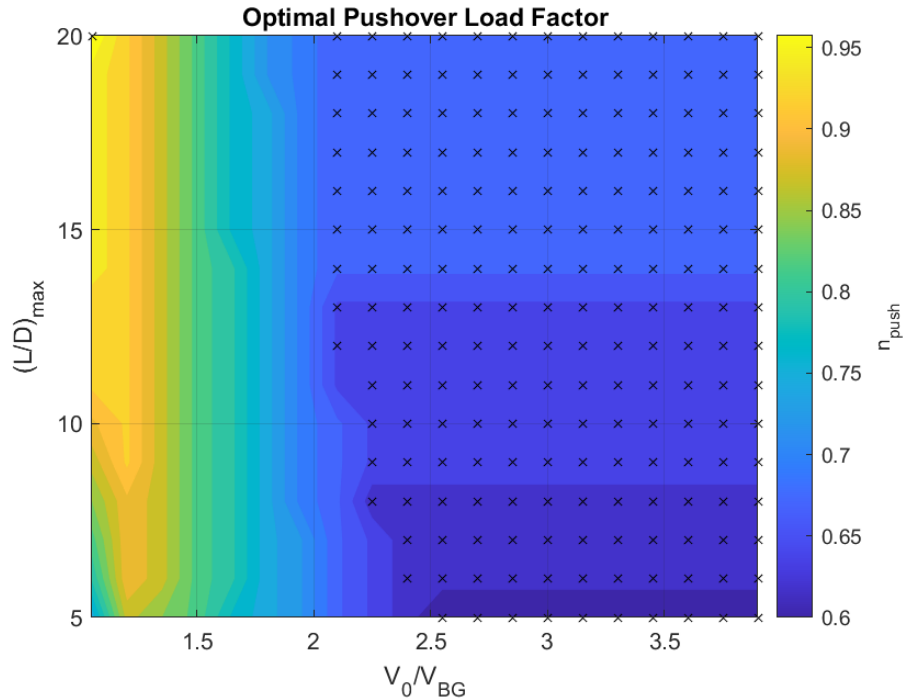


Figure 5(c). Optimal pushover load factor across the nondimensional regime map.

## 10. Verification and Sensitivity

Because the generalized map became the central result of the study, it was subjected to a separate verification and sensitivity study rather than accepted on appearance alone. The nondimensional model was cross-checked against the earlier dimensional C172-like implementation, selected map points were recomputed at higher fidelity, solver tolerances were tightened, the optimizer was started from widely separated initial guesses, the no-zoom baseline was audited, and both lift capability and maneuver constraints were varied.

| Verification item                             | Result                                                                                                                                                                                         |
|-----------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Dimensional / nondimensional C172 cross-check | Both models produced a 256.8-ft advantage with $n_{\text{pull}} \approx 2.0$ , $\gamma_{\text{zoom}} \approx 14^\circ$ , and $n_{\text{push}} \approx 0.78$ .                                  |
| ODE convergence                               | Changing RelTol from $10^{-6}$ to $10^{-10}$ produced no meaningful objective change.                                                                                                          |
| Energy consistency                            | Maximum reported energy residual below $1.7 \times 10^{-14}$ .                                                                                                                                 |
| Optimizer multistart                          | Seven widely separated starts plus the production-derived starting point converged within $3.9 \times 10^{-5}$ in absolute trajectory score; no significant competing local optimum was found. |
| High-fidelity map checks                      | Across 16 verification points, maximum absolute $\Delta J^*$ difference was 0.046; largest nontrivial percentage difference was about 2.7%.                                                    |
| Baseline audit                                | Passed: same initial state, finite deceleration and pushover, integrated drag, and identical $V_{BG} / \gamma_{BG}$ terminal state.                                                            |
| Lift-capability sensitivity                   | 315 optimized points over $\lambda = 1.25$ to 4.0 changed $\Delta J^*$ by at most $3.0 \times 10^{-6}$ ; maximum lift usage was 78%.                                                           |
| Constraint sensitivity                        | Trainer-like cases were nearly unchanged; high-speed cases changed materially as pull-G and zoom-angle limits were relaxed.                                                                    |

The lift-capability result is especially useful. The nominal value is  $\lambda = 1.62$ , but varying  $\lambda$  over a wide range had essentially no effect because none of the optimized trajectories approached  $CL_{max}$ . The current regime map is therefore not secretly controlled by a stall boundary. Under the tested maneuver constraints, initial-speed ratio and aerodynamic efficiency dominate the weak-to-moderate-speed behavior.

Maneuver limits matter at the opposite end of the map. At  $u_0 = 1.7$  and  $L/D = 9$ , the optimized nondimensional advantage changed only from 0.709 under conservative constraints to 0.710 under both nominal and aggressive constraints. At  $u_0 = 3.9$  and  $L/D = 18$ , however, the corresponding values were 39.2, 49.1, and 54.3. Of 36 nominal constraint-study points, 15 reached maximum pull load and 16 reached maximum zoom angle, while none reached a pushover or lift limit. The trainer-like result is therefore robust, whereas the exact magnitude of the high-energy result is increasingly maneuver-bound.

## 11. Human-Factors Opportunity Cost

The numerical optimization considers the airplane's trajectory, not the pilot's attention. In an actual engine failure, attention is also a finite resource. A precisely flown zoom requires control of pull-up load factor, flight-path angle, airspeed, pushover timing, and glide capture at the same time the pilot may need to select a landing area, diagnose or restart the engine, configure the aircraft, communicate, and maintain broader situational awareness. An aerodynamically superior trajectory can therefore be operationally inferior if the maneuver consumes more useful decision-making capacity than the additional energy state is worth.

The nominal trainer-case advantage is equivalent to only about 29 ft of additional best-glide altitude at 9:1. The study does not assign a numerical value to pilot attention, but it establishes the physical margin against which such a cost would have to be judged. At much higher excess-speed ratios, where the aerodynamic benefit becomes substantially larger, the trade may shift. The operational problem is therefore broader than maximizing aircraft energy alone; it is ultimately about maximizing the capability of the pilot-aircraft system to reach a successful outcome.

## 12. What the Study Does and Does Not Show

The simulation does not prove that pilots should routinely perform aggressive zoom climbs following engine failures, nor does it account for every consideration present in a real emergency, including terrain, reaction time, aircraft-specific procedures, structural limitations, propeller effects, changing configuration, pilot workload, stall/spin risk, or the need to maintain control while diagnosing the failure.

The aerodynamic models are simplified. The original aircraft representation uses a point mass and a parabolic drag polar, while the higher-speed experiments eventually require additional effects such as altitude, Mach number, compressibility, and aircraft-specific aerodynamic data before they should be interpreted quantitatively. No result from this study supersedes an aircraft flight manual or approved emergency procedure.

What the simulation does show is narrower but useful: the disposal of excess airspeed following a loss of thrust is fundamentally an energy and a trajectory problem. The statement “drag is high at high speed, therefore slow down as quickly as possible” is incomplete, and so is the statement “airspeed is energy, therefore zoom.” The generalized results show a smooth dependence on excess-speed ratio and aerodynamic efficiency, while the sensitivity studies clarify where maneuver constraints begin to control the answer. None of those findings removes the operational importance of aircraft procedures, terrain, workload, or pilot judgment.

### 13. Implications for Pilot Training

The most useful training implication may not be a new maneuver at all; it may simply be a better mental model. Power loss does not immediately transform an airplane into a glider traveling at best-glide speed. At the instant thrust disappears, the airplane possesses a particular combination of altitude and kinetic energy, and the pilot then influences how that energy is redistributed and how much is lost to drag. Statements such as “pitch for best glide” are useful operational shorthand, but they should not obscure the underlying mechanics.

The simulations also emphasize that a zoom, if used, is not merely a pitch-up maneuver; it is a complete trajectory. The pull-up, climb portion, pushover, and interception of the final glide all matter, and a poorly terminated zoom can sacrifice much of the theoretical gain or drive the airplane well below its intended glide speed.

For trainers operating only moderately above best glide, execution sensitivity and human workload may matter more in practice than the small theoretical improvement available from perfect optimization. The verified nondimensional map supports that conclusion: trainer-like conditions occupy a weak-benefit region that is numerically robust and largely insensitive to lift capability or reasonable changes in maneuver bounds. Faster and more aerodynamically efficient airplanes can occupy a much stronger energy-conversion regime, but the exact optimum there becomes increasingly dependent on permissible maneuver aggressiveness.

### 14. Future Work

The next useful extensions of the study include:

- repeating the validated nondimensional framework with aircraft-specific models and representative operating points, while adding altitude, true airspeed, Mach number, and compressibility where required;
- improving propeller drag and windmilling models, including stopped, windmilling, and feathered propeller states;
- developing a human-factors extension that treats maneuver time and workload as opportunity costs, then applying it to reaction delay, terrain geometry, landing-site selection, and comparison with practical pilot techniques and published emergency procedures.

### 15. Conclusion

This study began with a simple question: after an engine failure above best-glide speed, is it better to remain level and decelerate, or to zoom and convert some of the excess speed into altitude?

The answer produced by the model remains 'it depends,' but the dependence is now much better defined. For the modeled parabolic-polar family, optimized zoom benefit approaches zero as  $V_0/V_{BG}$  approaches one and rises smoothly with both excess-speed ratio and maximum glide ratio. The 110-to-65-kt trainer case is not an exception or numerical accident; it lies firmly within the weak-benefit region identified by both the dimensional and nondimensional analyses.

For the modeled 172-like trainer beginning at 110 knots and transitioning to a 65-knot best glide, the best trajectory uses a modest zoom and a timely pushover, but the retained range is small enough that execution error, wind, workload, and other operational considerations can become comparable to the aerodynamic gain. At substantially larger  $V_0/V_{BG}$ , the value of converting kinetic energy to altitude grows quickly. In that high-energy region the qualitative advantage remains strong, while the exact magnitude becomes increasingly controlled by allowable pull load factor and zoom angle.

Absolute airspeed alone should therefore not be interpreted as an indicator of zoom benefit. Higher-performance and larger aircraft generally also have higher best-glide speeds, so their greater cruise speeds do not necessarily imply a correspondingly larger excess-energy ratio. The relevant comparison

is primarily the initial speed relative to the aircraft's own best-glide speed,  $V_0/V_{BG}$ , together with its aerodynamic efficiency and applicable maneuver constraints. A faster aircraft may therefore occupy the same weak-benefit regime as a slower aircraft if both begin at similar multiples of their respective best-glide speeds.

The broader conclusion is therefore not 'zoom' or 'do not zoom.' Excess airspeed is an energy resource, but the useful disposition of that resource depends on the complete constrained trajectory and the operating regime. An emergency maneuver should not necessarily maximize aircraft energy alone. Instead it should maximize the pilot-aircraft system's ability to reach a successful outcome. That is a less convenient answer than a slogan, but it is also a more faithful description of what the airplane is actually doing.

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